

* Since most pipe flow designs use turbulent flow, there is not much information about $k = k(Re)$. You can almost always assume it will be turbulent flow if k will be a function of geometry (e.g. β) or a constant.

Example: calculate the pressure drop in a pipe with:

$$D = 0.1 \text{ m}, L = 50 \text{ m}, Q = 0.016 \text{ m}^3/\text{s}, g = 10^3 \text{ kg/m}^3$$

$$14 \text{ elbow joints}, \mu = 10^{-3} \text{ kg/m}\cdot\text{s}$$

* calculate $E_v, \text{tot} \rightarrow |\Delta P| = \frac{E_v}{Q}$

$$E_{v,\text{tot}} = \sum E_{v,i} = 14 \left(\frac{k_{\text{elbow}}}{2} w u^2 \right) + \frac{2L_f}{D} w u^2$$

$$|\Delta P| = 7 k_{\text{elbow}} g u^2 + \frac{2L_f}{D} g u^2 = \left(7 k_{\text{elbow}} + \frac{2L_f}{D} \right) g u^2$$

* Need u : $u = \frac{4Q}{\pi D^2} = \frac{4(0.016) \text{ m}^3/\text{s}}{\pi (0.1 \text{ m})^2} = 2.04 \text{ m/s}$

* Need Re : $Re = \frac{g u D}{\mu} = 2.04 \times 10^5$ (turbulent)

* Look up k_{elbow} : $k_{\text{elbow}} = 0.75$ (Table 12.1, p. 327 in Deen)

* calculate f : $f = [3.6 \log \left(\frac{Re}{64} \right)]^{-2}$

$$f = 0.0039$$

Notice: similar magnitude

$$|\Delta P| = \left(5.25 + \frac{2.50 \text{ m}}{0.1 \text{ m}} \cdot 0.0039 \right) \left(10^3 \frac{\text{kg}}{\text{m}^3} \cdot (2.04 \text{ m/s})^2 \right)$$

3.9

$$|\Delta P| = 3.81 \times 10^4 \text{ Pa} = \boxed{38.1 \text{ kPa}}$$